Additinal Exercise

Deadline of submission: February 20 (Tue), 2018

Let f be a function defined by

$$f(x,y) = \begin{cases} \frac{xy}{\sqrt{x^2 + y^2}} &, (x,y) \neq (0,0) \\ 0 &, (x,y) = (0,0) \end{cases}$$

Show that f is continuous but not differentiable at (0,0), although it has both partial derivatives existing there.